

CS-7863: Scientific and Statistical Computing  
Homework #1  
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**1.a)**

```
## Part A: compute binding energy
computeBindingEnergy <- function(A, Z){
  if (A %% 2 == 1) {
    spin <- 0
  }else if (A %% 2 == 0 && Z %% 2 == 0){
    spin <- 12
  }
  else {
    spin <- -12
  }

  return((15.67*A) -
    (17.23*(A^(2/3))) -
    ((0.75)*((Z^2)/(A^(1/3)))) -
    ((93.2)*(((A-(2*Z))^2)/A)) +
    (spin/(A^(1/2))))
}
```

**1.b)**

```
## Part B: compute Z=28 and A=58
# Nickel
bind.energy <- computeBindingEnergy(58,28)
cat(round(bind.energy,digits=2),"MeV")
```

493.94 MeV

### 1.c)

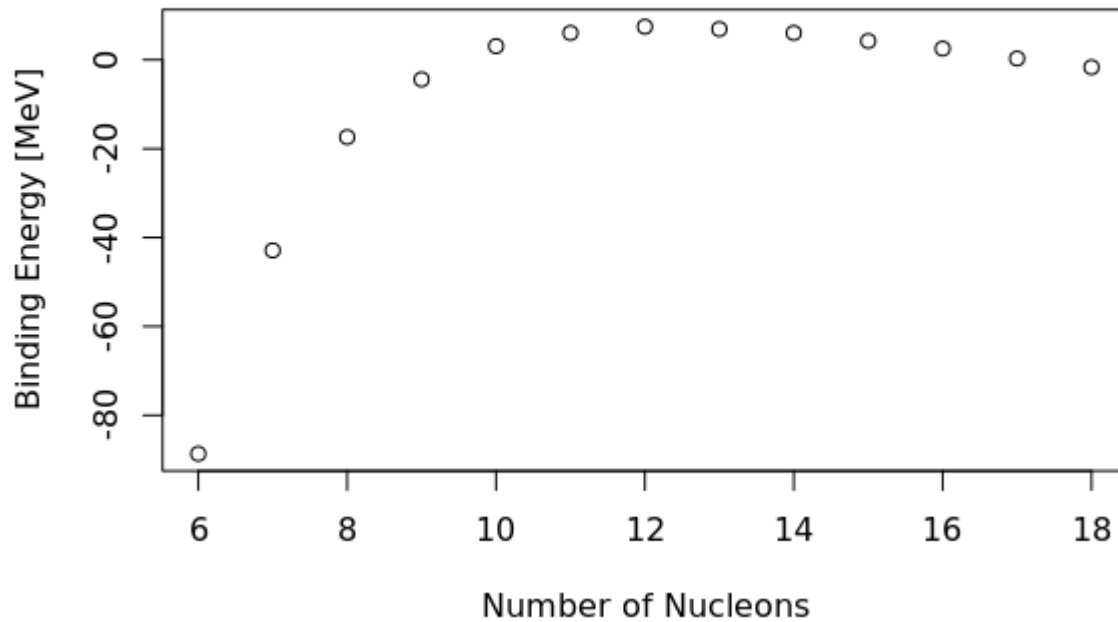
```
## Part C: table with two columns: nucleons and binding energy per
nucleon
Z=6 # Carbon
carbon_df <- data.frame(nrow=2*Z, ncol=2)
for (i in seq(Z, 3*Z)){
  # +1 since R indexes at 1
  carbon_df[i-Z+1,] <- rbind(i, computeBindingEnergy(i, Z)/i)
}
rownames(carbon_df) <- NULL
colnames(carbon_df) <- c("A", "B/A")
print(carbon_df, row.names=FALSE)
# Get max binding energy row
print(carbon_df[which.max(carbon_df$"B/A"),], row.names=FALSE)

plot(carbon_df$A, carbon_df$"B/A", xlab="Number of Nucleons",
      ylab="Binding Energy [MeV]",
      main="Number of Nucleons on Binding Energy for Carbon")
```

| A  | B/A         |
|----|-------------|
| 6  | -88.6719833 |
| 7  | -42.9044922 |
| 8  | -17.4021699 |
| 9  | -4.4111252  |
| 10 | 3.0707868   |
| 11 | 6.0487081   |
| 12 | 7.4500014   |
| 13 | 6.9074722   |
| 14 | 6.0478948   |
| 15 | 4.2257131   |
| 16 | 2.5250851   |
| 17 | 0.2890953   |
| 18 | -1.6752533  |

```
> print(carbon_df[which.max(carbon_df$"B/A"),], row.names=FALSE)
A    B/A
12 7.450001
```

## Number of Nucleons on Binding Energy for Carbon



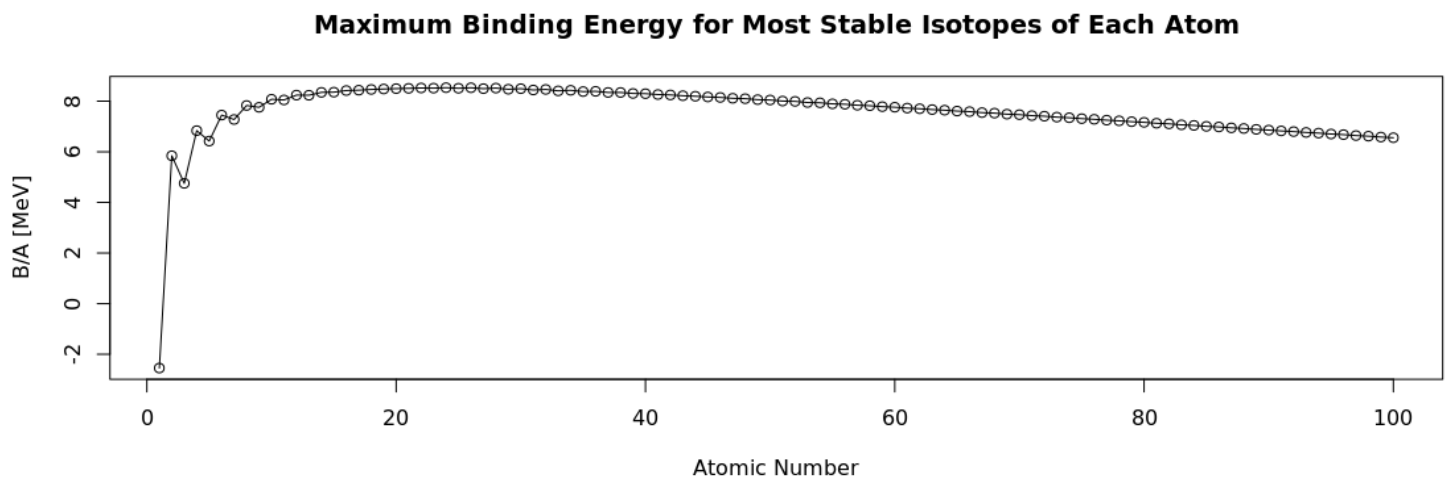
### 1.d)

```
## Part D: find the value of A that gives the maximum binding energy
computeMaxBind <- function(Z){
  maxBind <- -Inf
  A.maxBind <- -Inf
  for (i in seq(Z, 3*Z)){
    binde <- computeBindingEnergy(i, Z)/i
    if (binde > maxBind){
      maxBind <- binde
      A.maxBind <- i
    }
  }
  return(c(A.maxBind, maxBind))
}
```

1.e)

```
bounds <- 100
binding_df <- data.frame(nrow=bounds, ncol=2)
for (i in seq(1, bounds)){
  binding_df[i,] <- c(i, computeMaxBind(i)[2])
}

plot(binding_df, xlab="Atomic Number", ylab="B/A [MeV]", type="o",
      main="Maximum Binding Energy for Most Stable Isotopes of Each Atom")
```



```
# Z with largest binding energy
print(binding_df[which.max(unlist(binding_df[2])),], row.names=FALSE)
```

| nrow | ncol     |
|------|----------|
| 24   | 8.532623 |